Problem E. Concave Hull

Time limit:	3 seconds
Memory limit:	1024 megabytes

You are given n points on the plane; the coordinates of the i-th point are (x_i, y_i).

A Concave Hull is a simple polygon (meaning it has no self-intersections) such that the set of vertices is a non-empty subset of the given n points, and all the n points lie inside or on the boundary of the polygon. Exactly one of the interior angles of the polygon is greater than π, and all the other angles are less than π.

Calculate twice the sum of the area of all the Concave Hulls of the given set of points. Since the answer might be large, output it modulo $10^9 + 7$.

Input

The first line contains one integer n ($3 \le n \le 2 \cdot 10^3$), denoting the number of points.

The i-th of the following n lines contains two integers x_i, y_i ($0 \le x_i, y_i \le 10^9$), denoting the coordinates of the i-th point.

It is guaranteed that the n points are pairwise distinct, and no three points are collinear.

Output

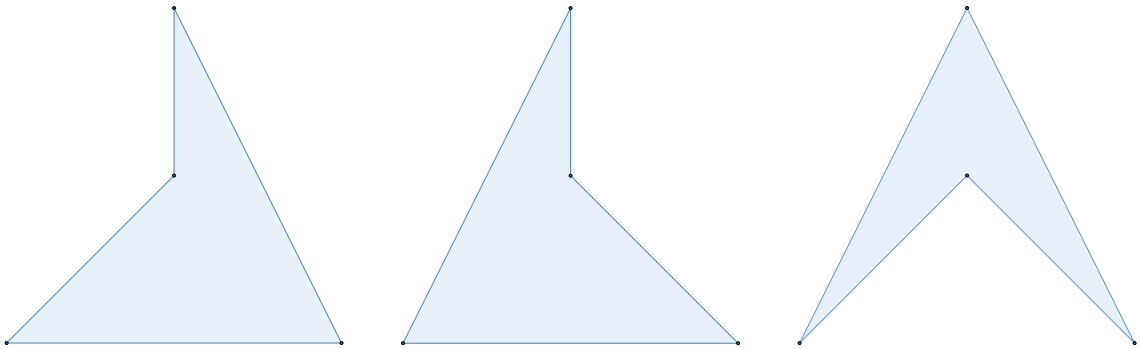
Output a single integer in one line, denoting twice the sum of the area of the Concave Hulls modulo $10^9 + 7$.

Examples

standard input	standard output
4 0 0 2 0 1 2 1 1	8
15 3442 3341 3136 3120 3228 3113 3143 2981 3050 3052 2970 2973 2964 3011 2921 2927 2844 2715 2655 2661 2666 2637 2755 2731 2657 2684 2662 2629 2542 2508	23993862

Note

For the first sample, there are three Concave Hulls.



the area is 1.5 the area is 1.5 the area is 1

So the total area is 4, and the answer is $4 \times 2 = 8$.