Problem H
Hextech High-roll
Time limit: 2 seconds

Jayce is playing a game of *ARAM: Mayhem*. He has reached the Augment Selection phase and is looking for the perfect augmentation to carry his team. Specifically, he is desperately hunting for the Golden augment known as *Slow and Steady*.



The Game UI for card selection. Oops, it looks like Jayce cannot find *Slow and Steady* in the Prismatic pool...

Currently, the game interface presents k augment cards to Jayce. While each card has a different effect, to Jayce, the i-th visible card is worth a_i value points. There is a hidden pool of n other augment cards waiting in the deck. The value points of these cards are known to be the multiset $\{b_1, b_2, \ldots, b_n\}$, but their order is shuffled uniformly at random.

Jayce can refresh each of the k card slots **at most once**. The process works as follows:

- There are individual reroll buttons under each of the k cards (as shown in the game UI).
- Jayce can choose a slot that hasn't been rerolled yet, discard the current card, and draw the top card from the deck to replace it.
- Jayce sees the result of a reroll immediately before deciding his next move: whether to reroll another available slot, or stop.

At the end of the process, Jayce will select one card among the k cards currently visible on the screen.

Jayce plays optimally to maximize the expected value of the card he eventually picks. Calculate this maximum expected power level.

Input

The first line contains two integers k and n ($1 \le k \le n \le 10^5$), indicating the number of visible slots and the number of cards in the deck.

The second line contains k integers $a_1, a_2, \ldots, a_k$ ($-10^5 \le a_i \le 10^5$), indicating the power levels of the initially visible cards.

The third line contains n integers $b_1, b_2, \ldots, b_n$ ($-10^5 \le b_i \le 10^5$), indicating the power levels of the cards in the deck.

Output

Output the maximum expected value of the card as a single decimal real number.

Your answer will be considered correct if its absolute or relative error does not exceed 10^{-4}. Formally speaking, suppose that your output is a and the jury's answer is b, your output is accepted if and only if $\frac{|a-b|}{\max(1,|b|)} \le 10^{-4}$.

Sample Input 1

```
1 2
10
1 100
```

Sample Output 1

```
50.5
```

Sample Input 2

```
3 5
3 4 7
1 2 3 5 8
```

Sample Output 2

```
7.4
```

Sample Input 3

```
2 4
-1 -2
-3 -4 -5 -6
```

Sample Output 3

```
-1
```

Sample Input 4

```
5 14
1 3 5 7 9
-1 -1 0 0 2 2 4 4 6 6 8 8 10 10
```

Sample Output 4

```
9.505494505
```